

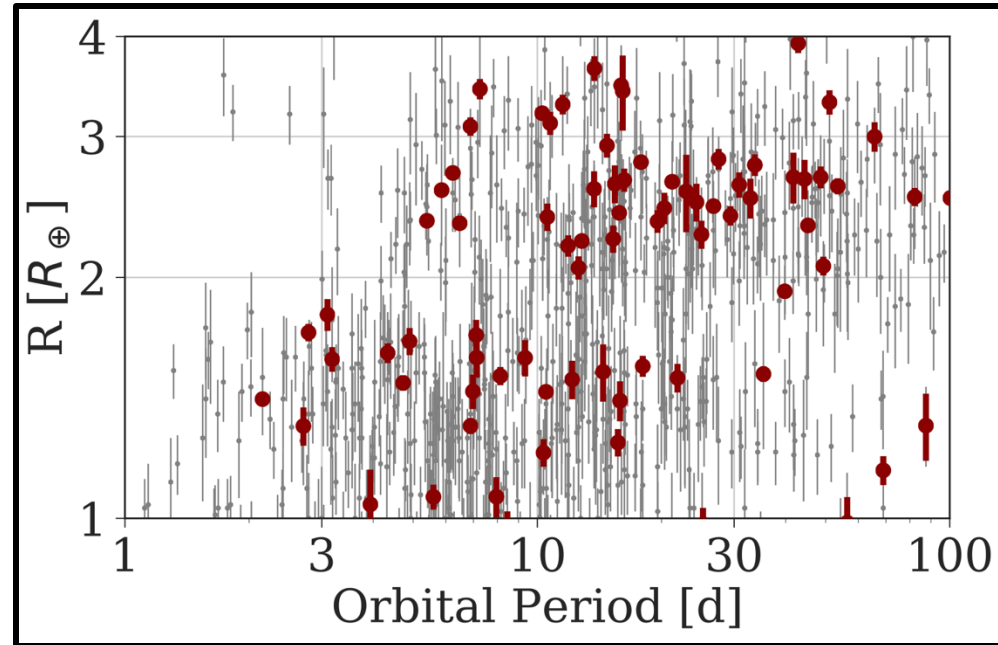


THE UNIVERSITY OF  
SYDNEY

# Should We Trust the Asteroseismic Scaling Relations?

Tim Bedding (Univ. Sydney)

The radius valley

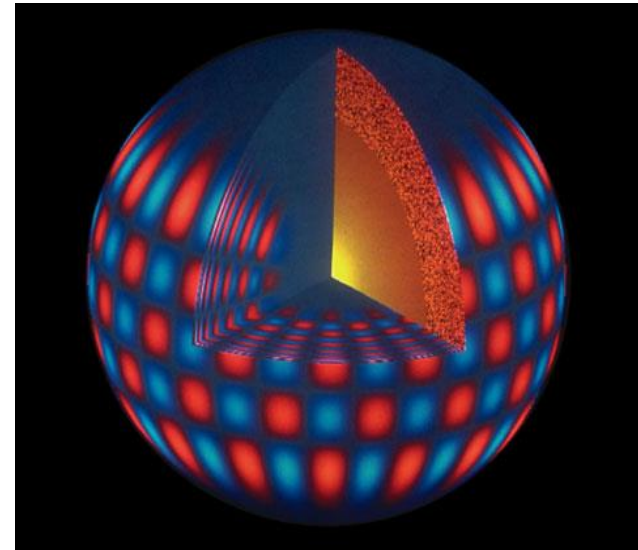
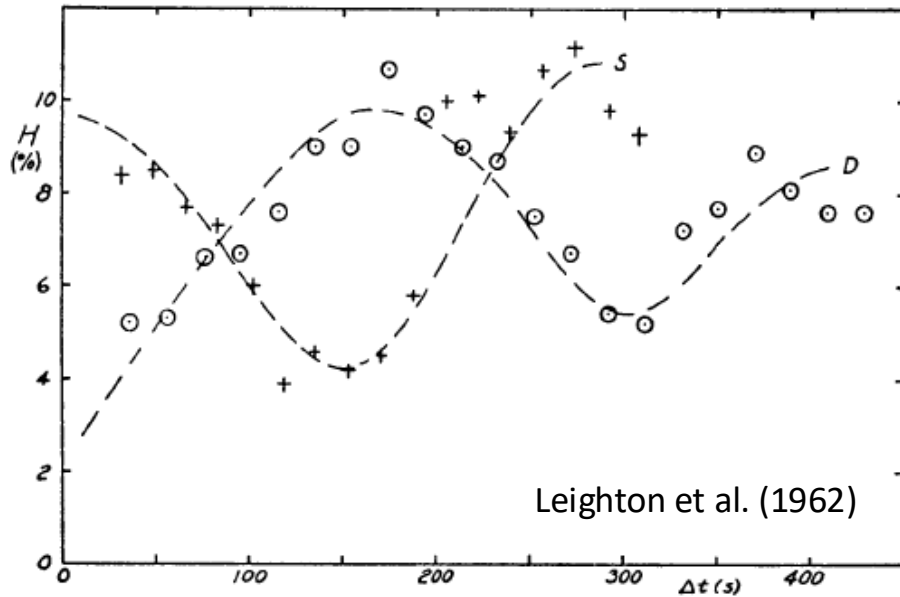


Van Eylen et al. (2017)

# The discovery of 5-minute oscillations in the Sun

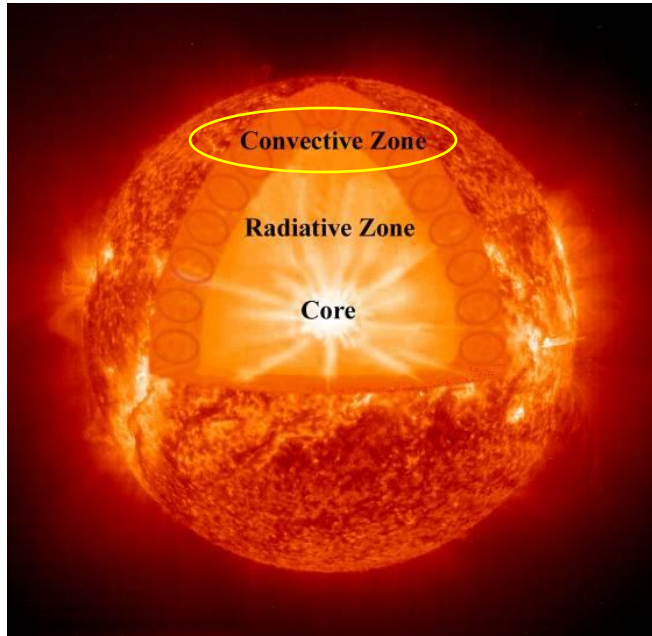
## VELOCITY FIELDS IN THE SOLAR ATMOSPHERE I. PRELIMINARY REPORT\*

ROBERT B. LEIGHTON, ROBERT W. NOYES, AND GEORGE W. SIMON  
California Institute of Technology, Pasadena, California

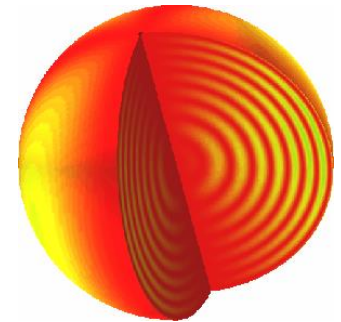
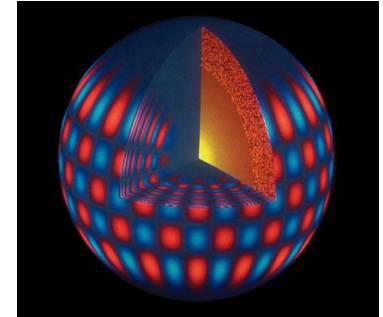
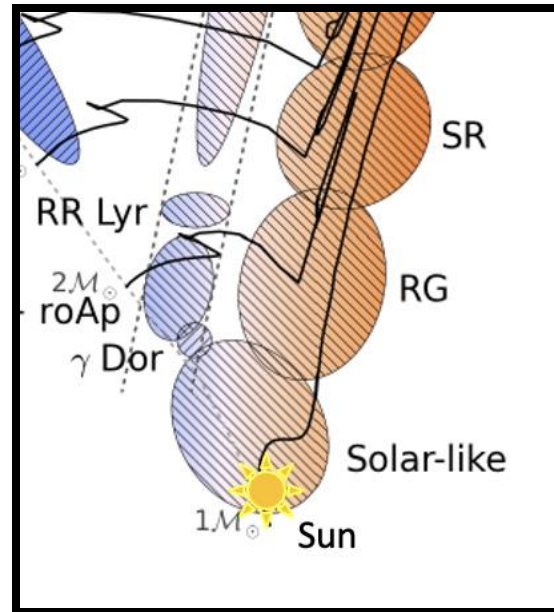


a high-degree mode ( $\ell=20$ )

# What drives solar-like oscillations?



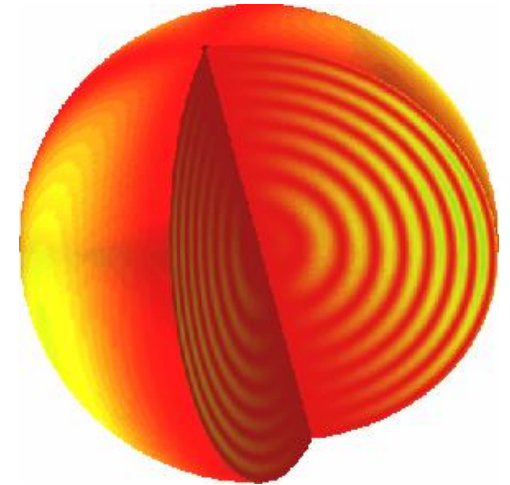
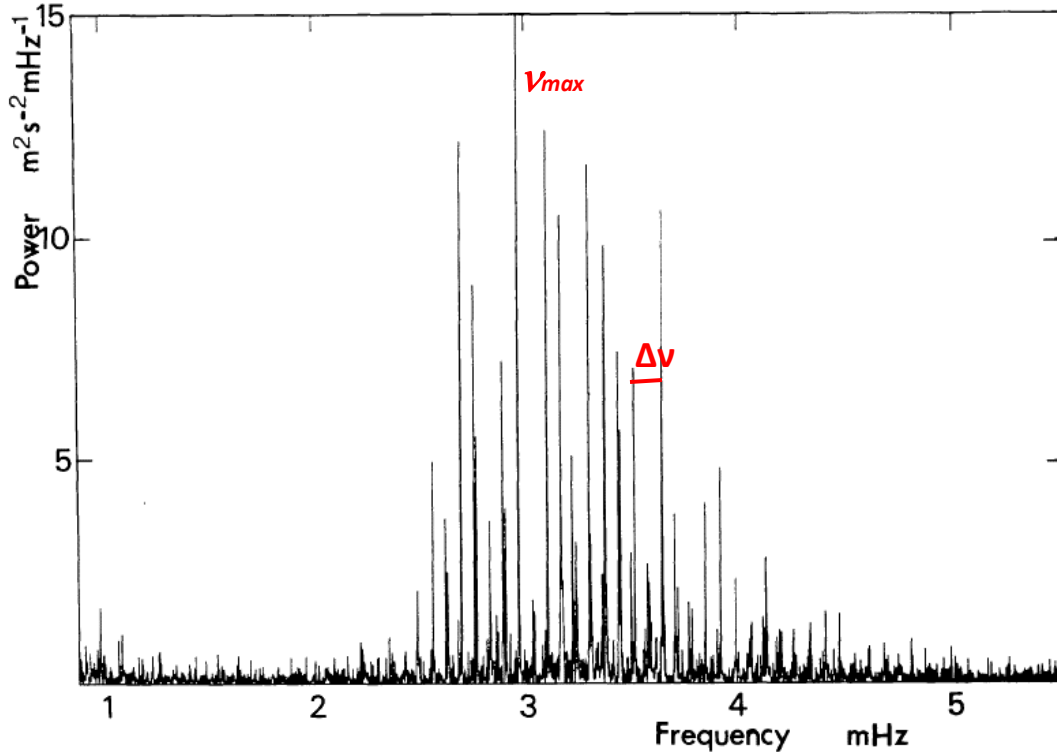
Convection excites many standing sound waves (stochastic process)



# Sun-as-a-star helioseismology

FULL-DISK OBSERVATIONS OF SOLAR OSCILLATIONS FROM  
THE GEOGRAPHIC SOUTH POLE: LATEST RESULTS\*

Grec et al. (1983)



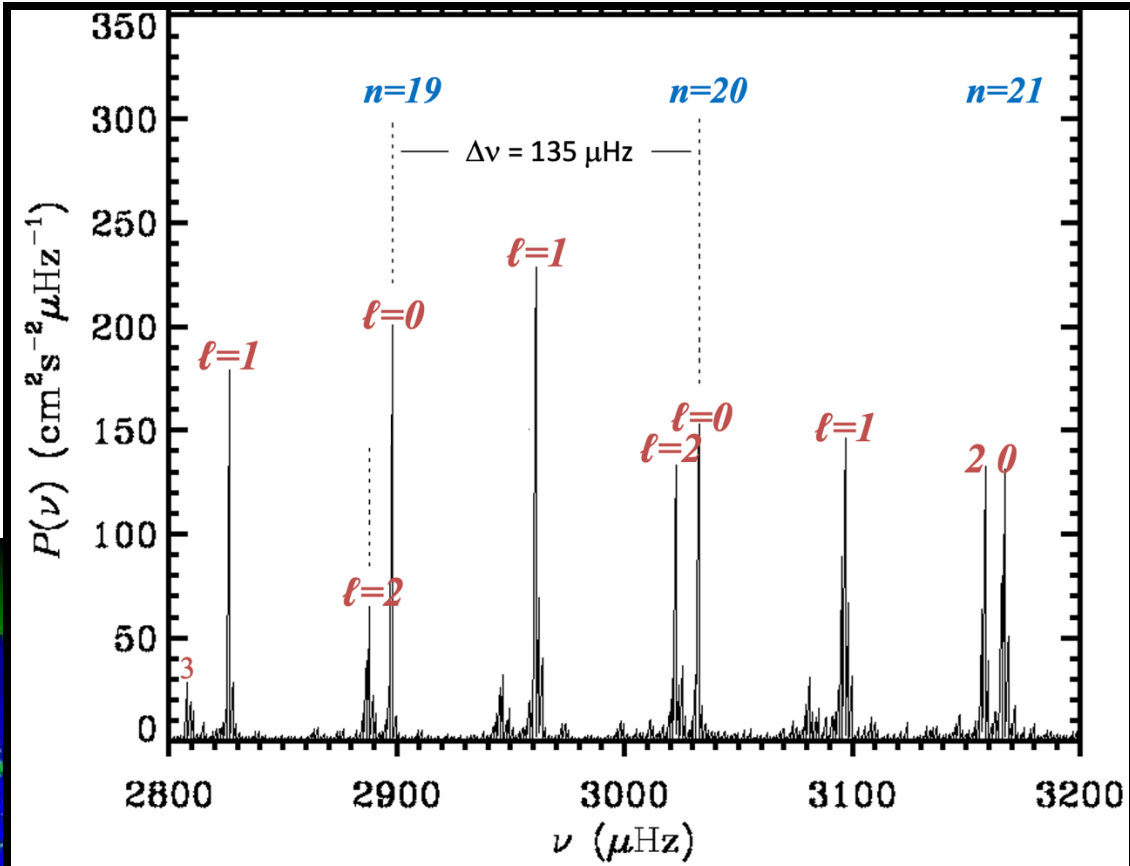
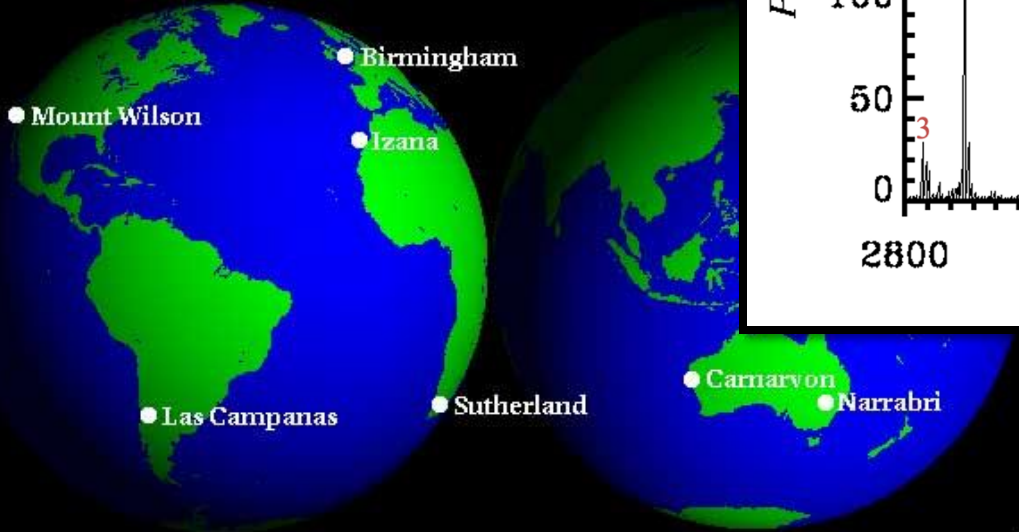
a low-degree mode ( $\ell=2$ )

# The Sun

Birmingham Solar Oscillations Network  
**BiSON**

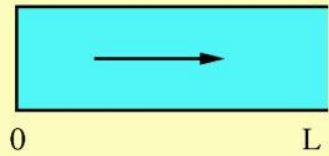


UNIVERSITY OF  
BIRMINGHAM

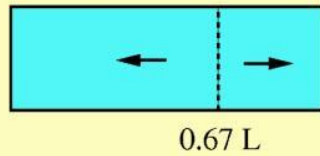


# p-mode oscillations are standing sound waves

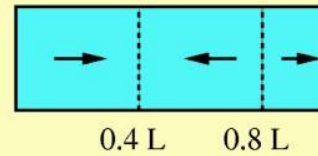
----- nodal line  
————— motion of gas



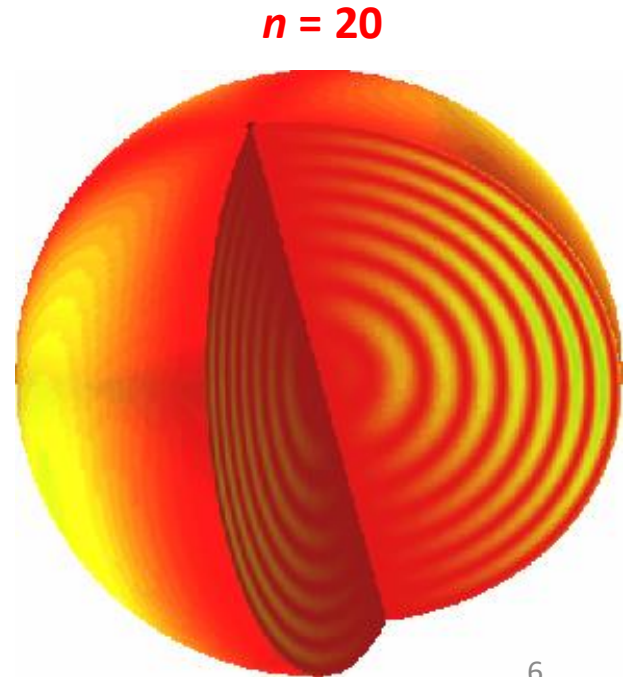
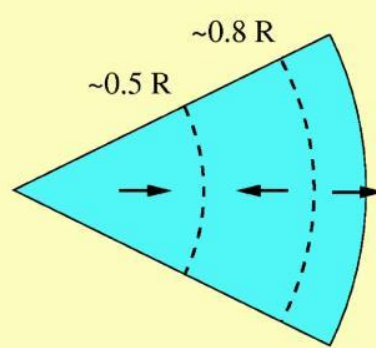
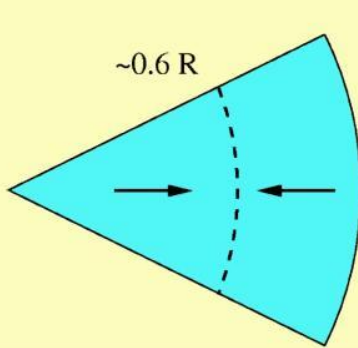
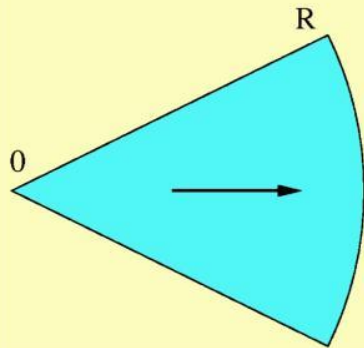
$n = 1$



$n = 2$

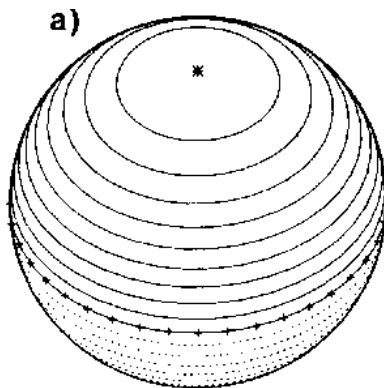
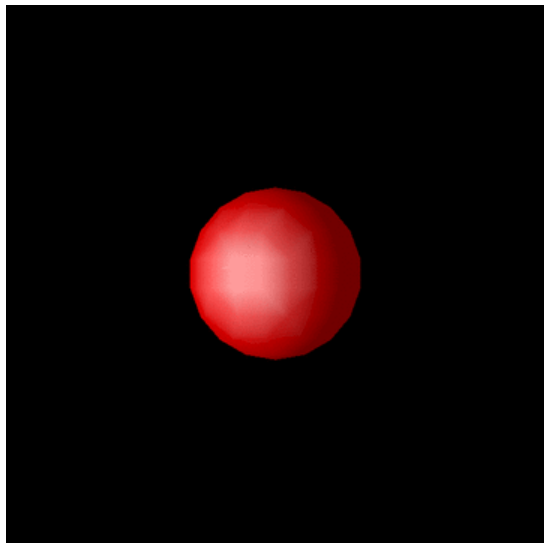


$n = 3$

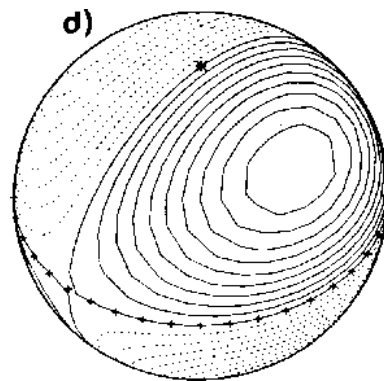
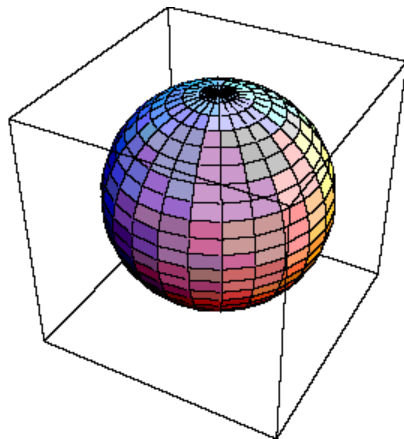


$n$  is the *radial order* of the overtone

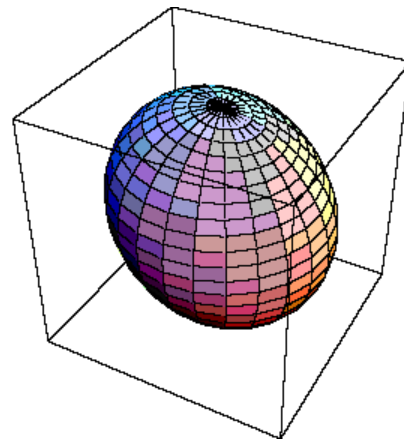
$\ell = 0$  (radial modes)



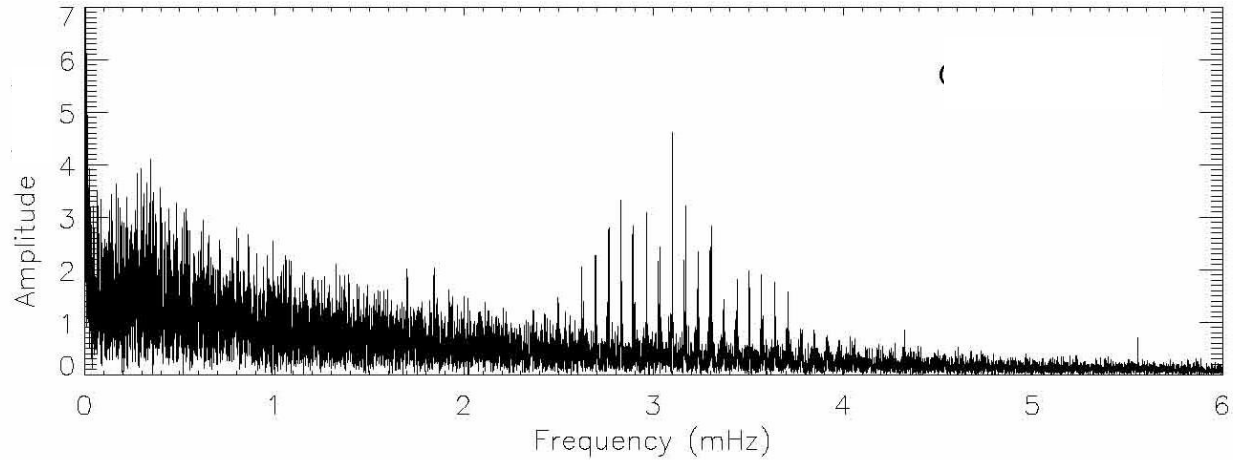
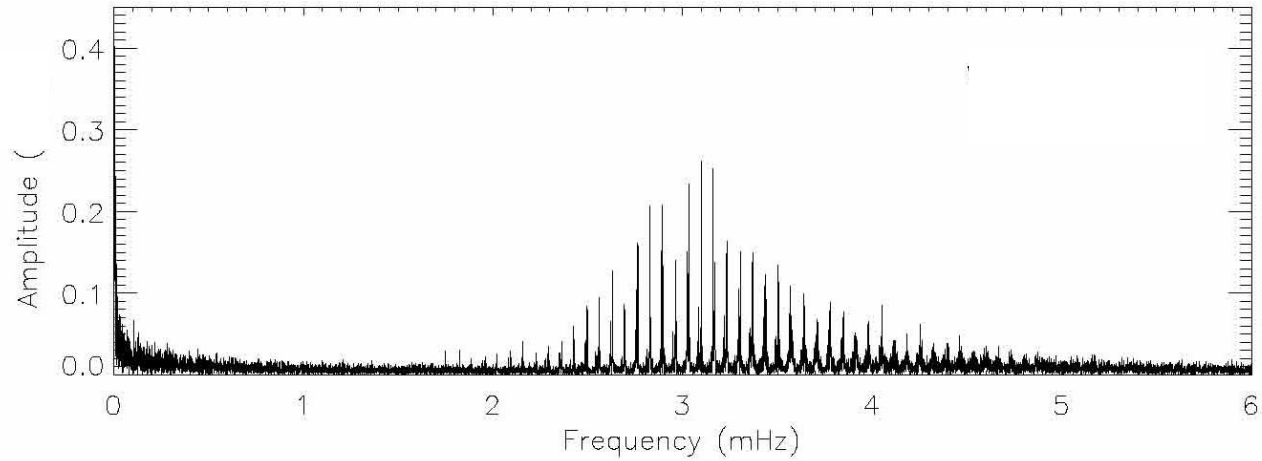
$\ell=1$



$\ell=2$

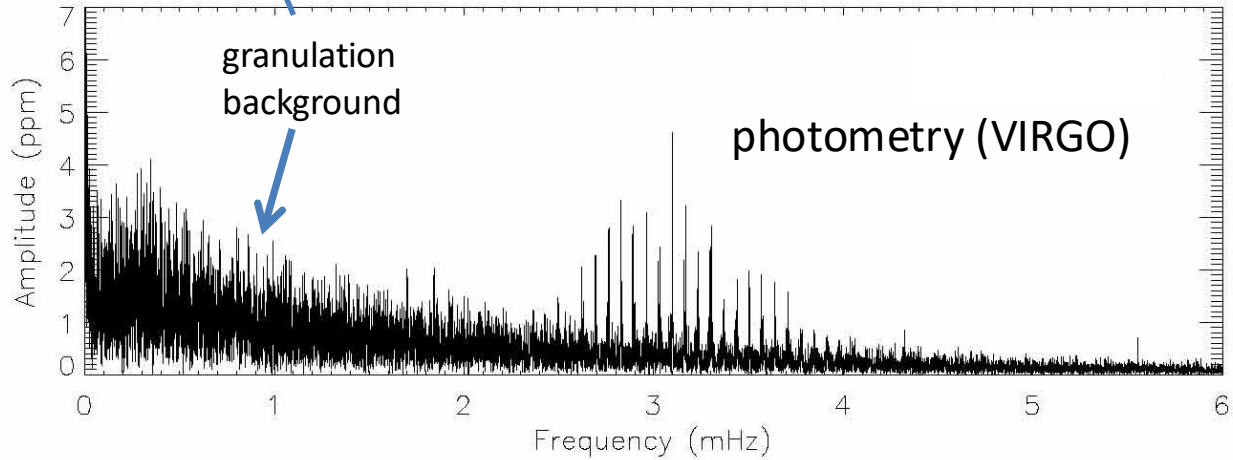
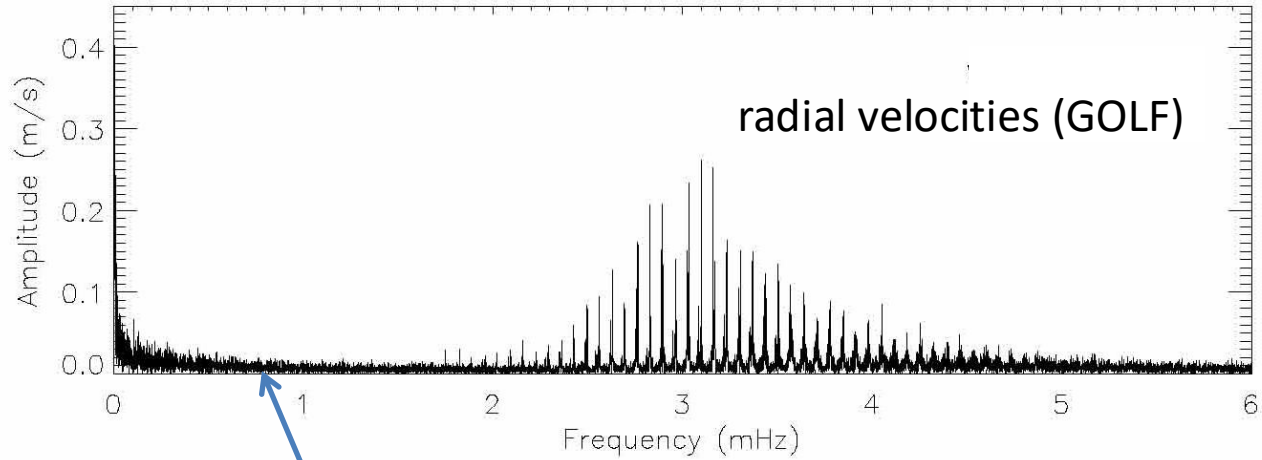


# Sun (20 days with SOHO)





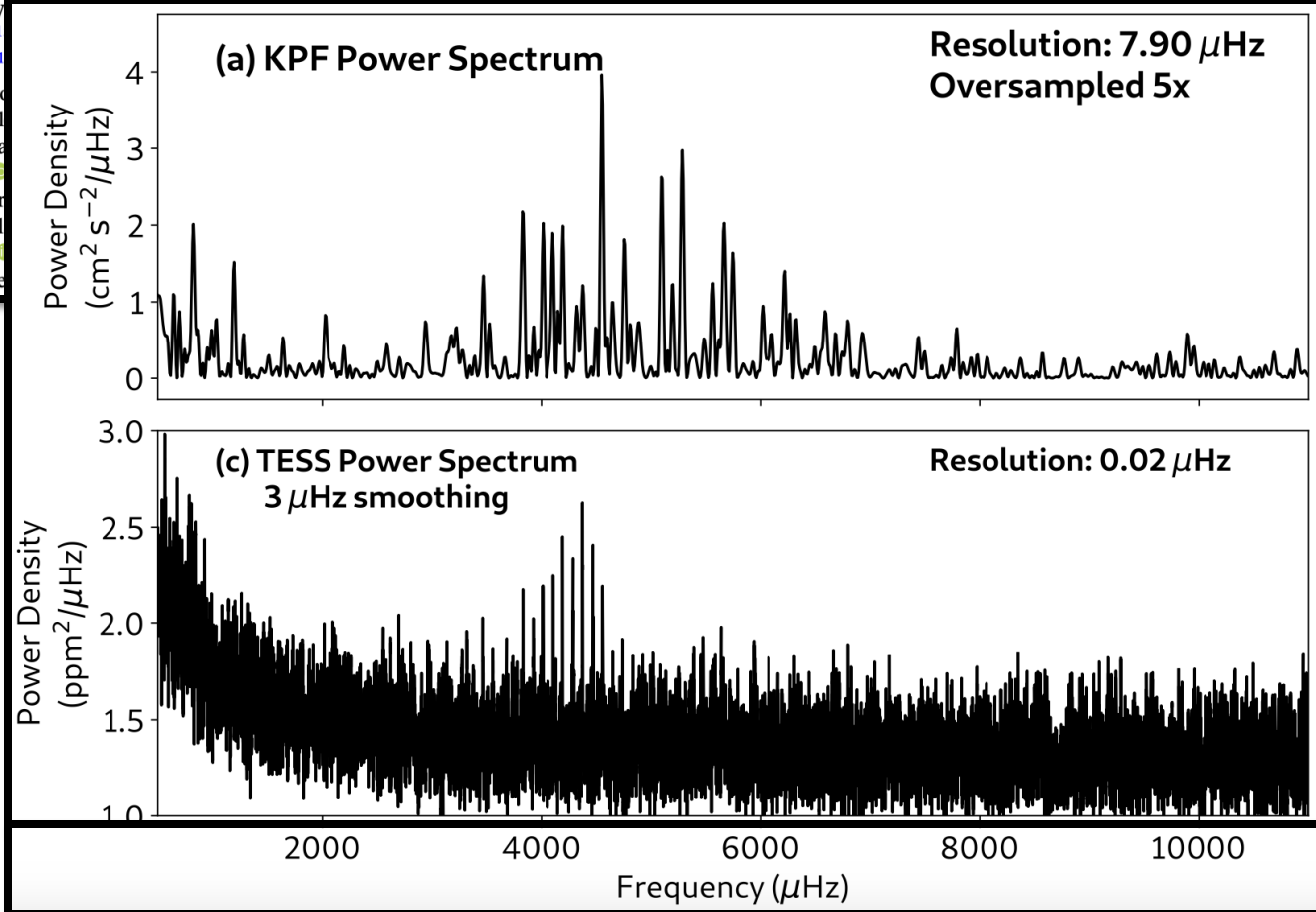
# Sun (20 days with SOHO)



# Asteroseismology of the Nearby K Dwarf $\sigma$ Draconis Using the Keck Planet Finder and TESS

(2024)

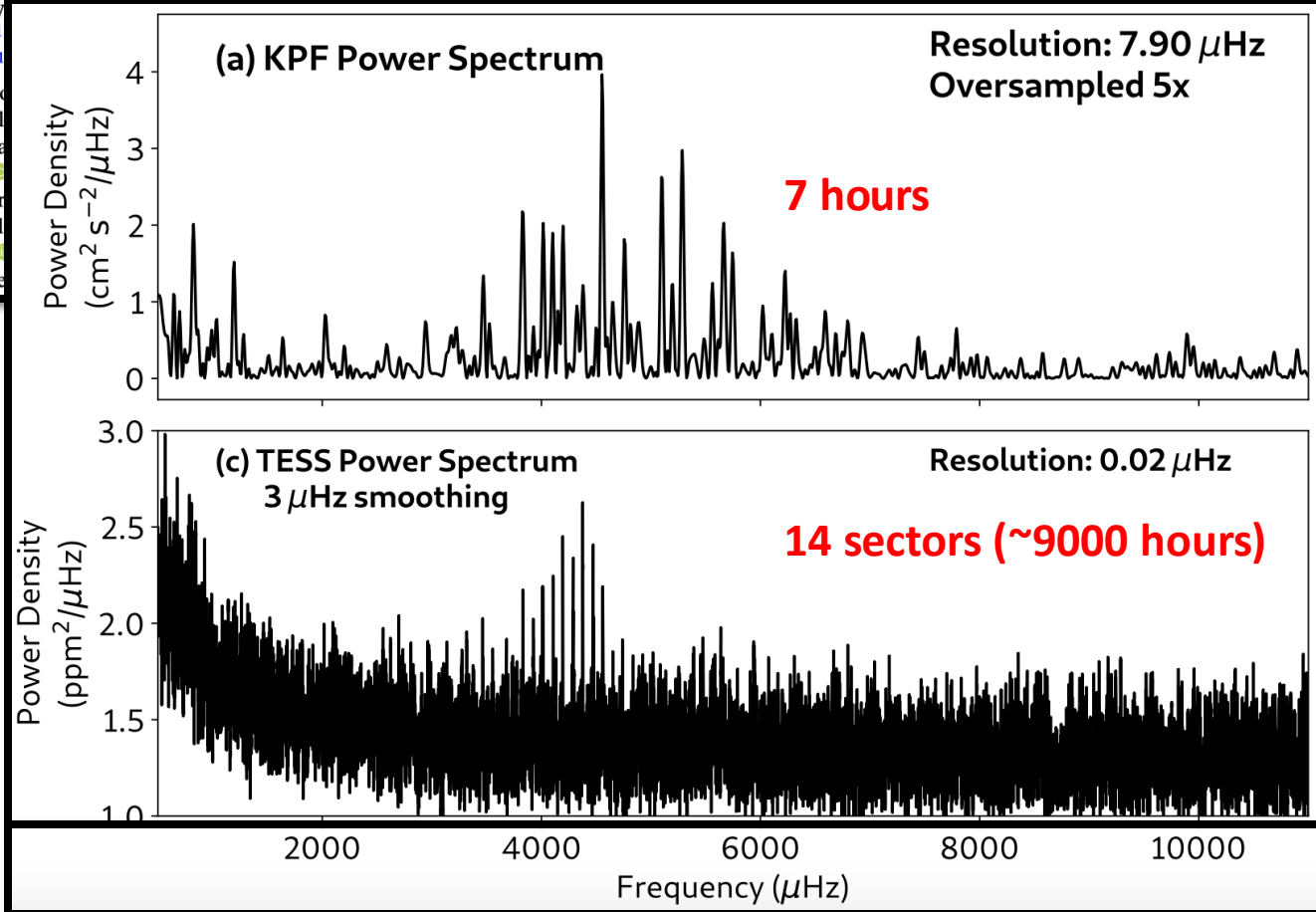
Marc Hon<sup>1,2</sup>, Daniel Huber<sup>2,3</sup>, Yaguang Li<sup>2</sup>, Travis S. Metcalfe<sup>4</sup>, Timothy R. Bedding<sup>3</sup>, Joel Ong<sup>2</sup>, Ashley Chontos<sup>2,5</sup>, Ryan Rubenzahl<sup>6</sup>, Samuel Halverson<sup>7</sup>, Rafael A. García<sup>8</sup>, Hans Kjeldsen<sup>9</sup>, Dennis Stello<sup>3,10,11</sup>, Daniel R. Hey<sup>2</sup>, Tiago Campante<sup>12,13</sup>, Andrew W. Azzaro<sup>14</sup>, Ashley D. Baker<sup>14</sup>, Jerry Edelstein<sup>15</sup>, Chris Smith<sup>1</sup>, Matt Brown<sup>17</sup>, Dwight Chan<sup>17</sup>, Fei Dai<sup>2</sup>, William Deich<sup>1</sup>, Bradford Holden<sup>18</sup>, Aaron Householder<sup>1,19</sup>, Heungsik Hwang<sup>20</sup>, Marc Kassis<sup>17</sup>, Stephen Kaye<sup>14</sup>, Russ Laher<sup>22</sup>, Kyle L. B. Marston<sup>21</sup>, Timothy N. Miller<sup>15</sup>, Joel Payne<sup>17</sup>, Erik A. Petigura<sup>23</sup>, Dale Sanford<sup>18</sup>, Christian Schwab<sup>24</sup>, Abby P. Shamm<sup>6</sup>, Adam Vandenberg<sup>17</sup>, Shin Ywan Wang<sup>22</sup>, Edward J. Weidner<sup>25</sup>, Sarbani Basu<sup>25</sup>, Megan Bedell<sup>26</sup>, Heather M. Cegla<sup>27</sup>, Heather Knutson<sup>6</sup>, Dimitri Mawet<sup>6</sup>, John O'Meara<sup>17</sup>, Sharon Xuesong Wang<sup>32</sup>, Lauren M. Weiss<sup>28</sup>

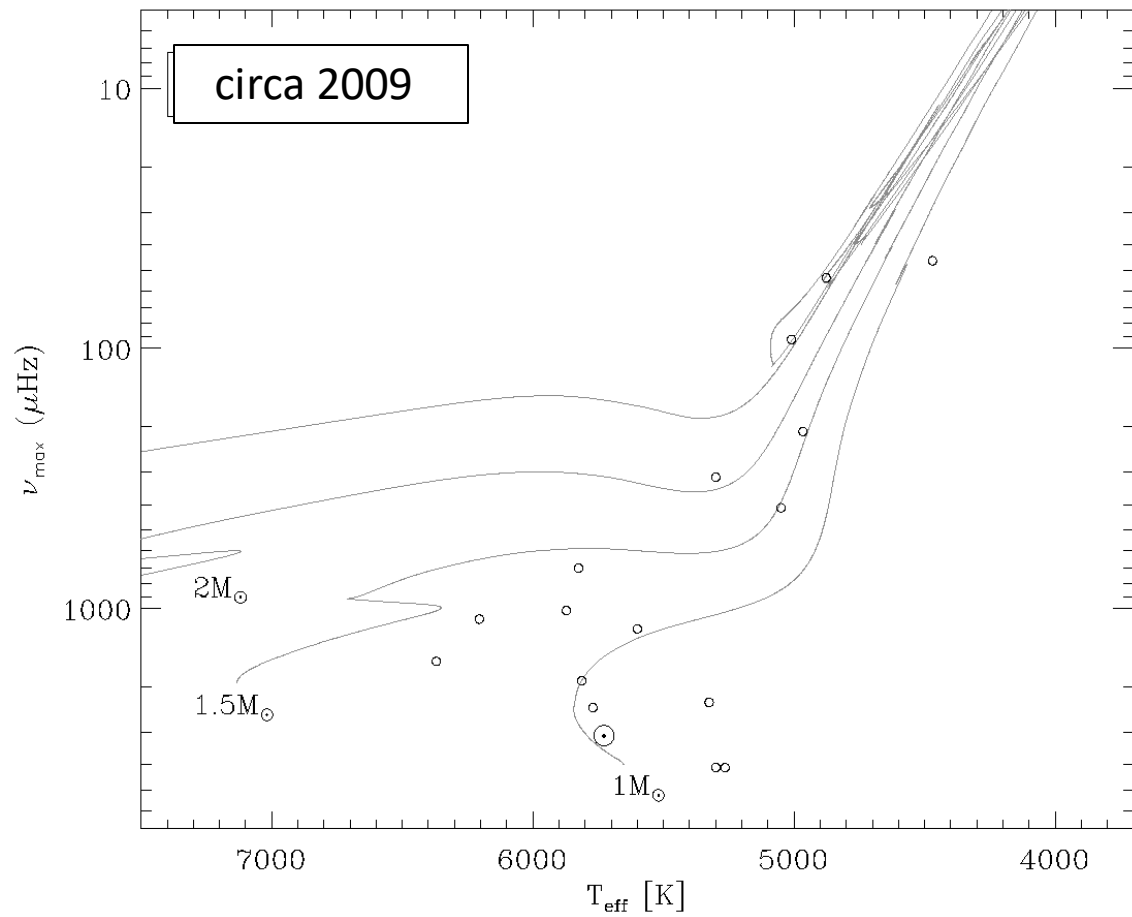


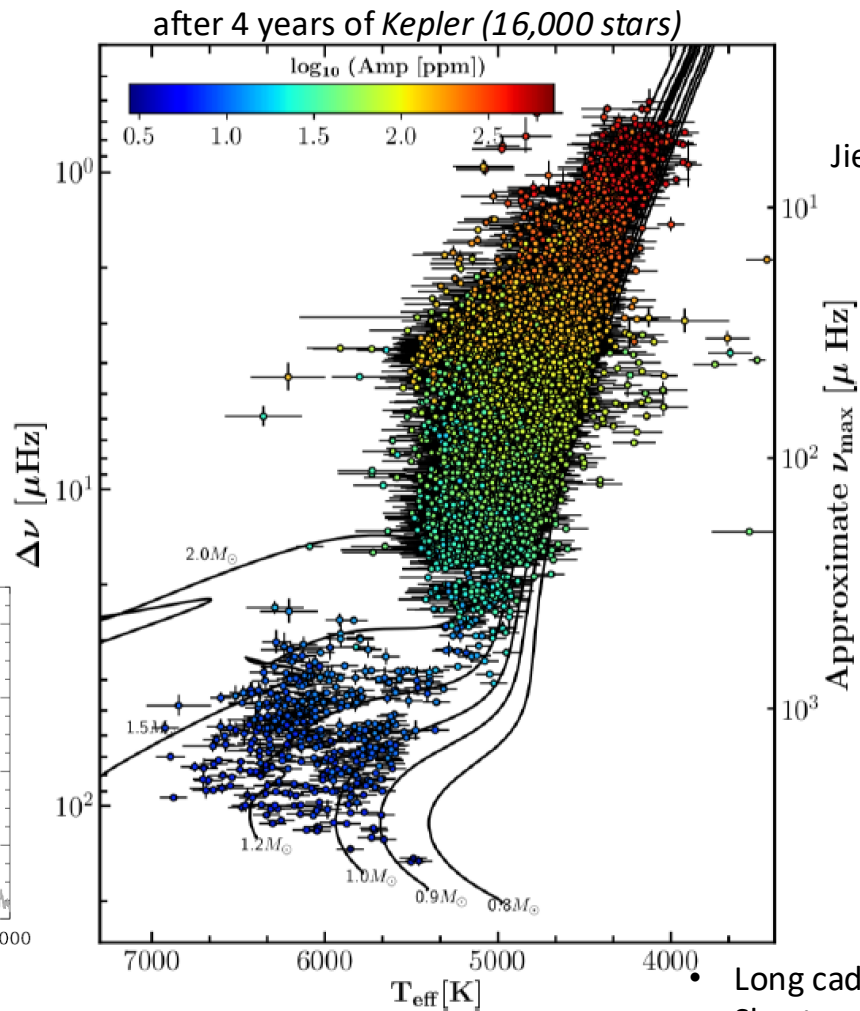
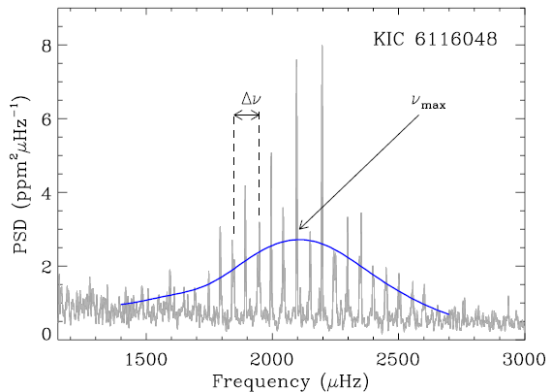
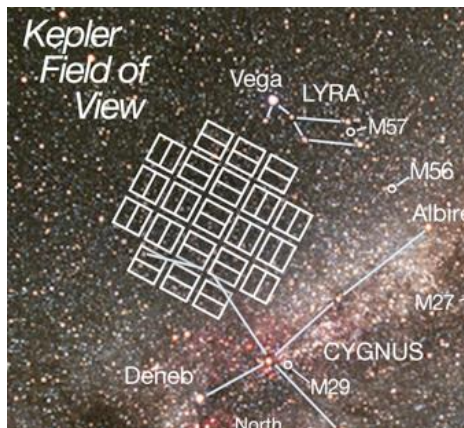
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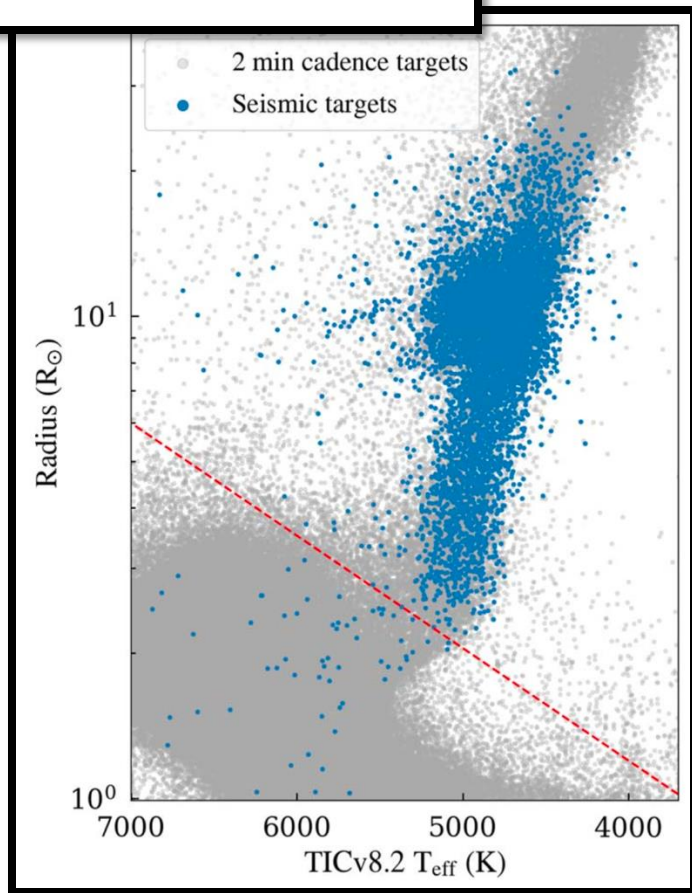
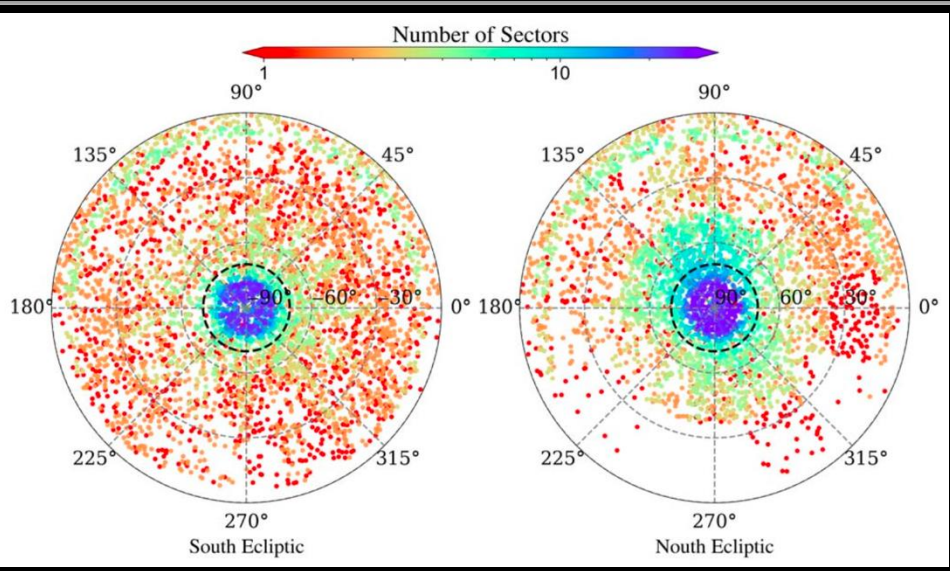


Jie Yu et al. (2017, 2018ab)

- Long cadence (29.4 minutes) – 150,000 stars
- Short cadence (1 minute) – 512 stars<sup>13</sup>

# Detection of Solar-like Oscillations in Subgiant and Red Giant Stars Using 2 minute Cadence TESS Data (2024)

Jianzhao Zhou<sup>1,2</sup> , Shaolan Bi<sup>1,2</sup> , Jie Yu<sup>3,4,5,6</sup> , Yaguang Li<sup>7,8</sup> , Xianfei Zhang<sup>1,2</sup> , Tanda Li<sup>1,2,9</sup> , Liu Long<sup>1,2</sup> , Mengjie Li<sup>1,2</sup>, Tiancheng Sun<sup>1,2</sup> , and Lifei Ye<sup>1,2</sup> 



**TESS solar-like oscillations:** Stello et al. (2022)  
Campante et al. (2019) Hatt et al. (2023)  
Mackereth et al. (2021) Malla et al. (2024)  
Hill et al. (2021) Ong et al. (2024)  
Grunblatt et al. (2021, 2022) Pope et al. (2024)  
Hon et al. (2021, 2022) Sreenivas et al. (submitted)

# Asteroseismic scaling relations:

1.  $\nu_{\max}$  depends on surface properties (excitation & damping of modes):
2.  $\Delta\nu$  scales with sqrt[mean density] (sound travel time across star):

$$\frac{\nu_{\max}}{\nu_{\max,\odot}} \approx \frac{g}{g_{\odot}} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{-1/2}$$

$$\Delta\nu \propto \left( \frac{M}{R^3} \right)^{1/2}$$

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Solve to get mass and radius:

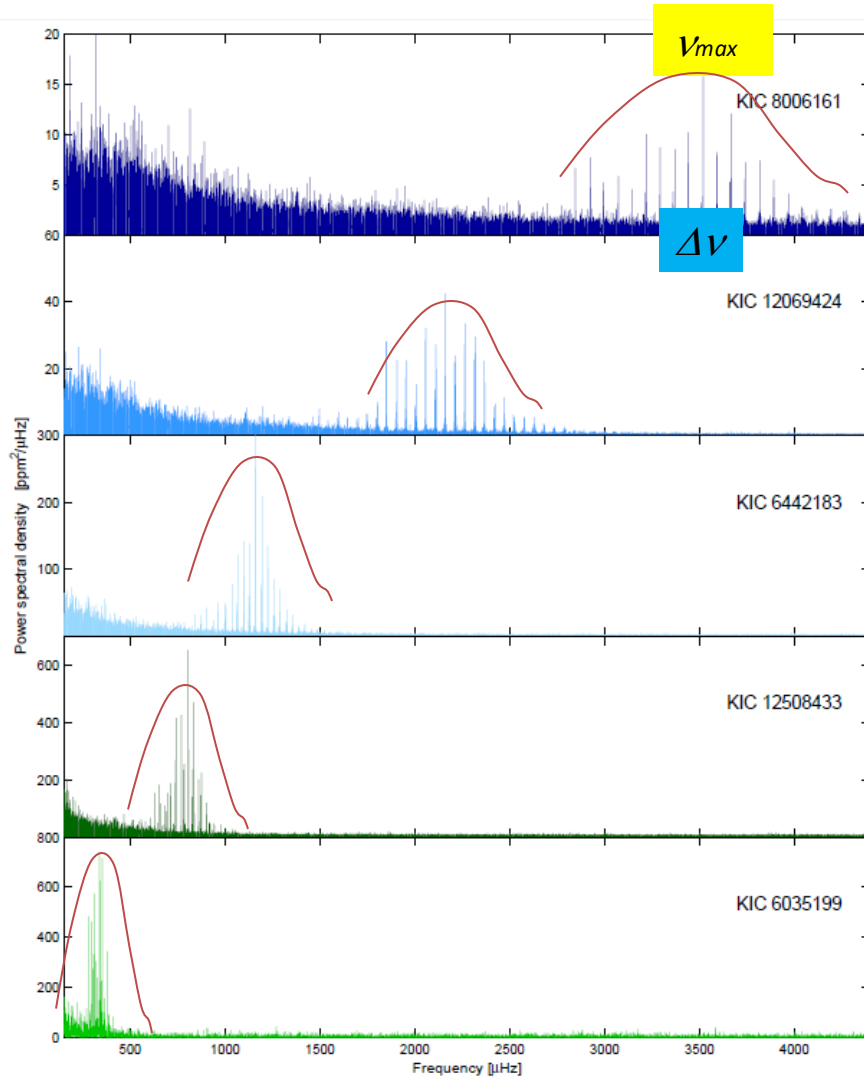
$$\frac{M}{M_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{3/2}$$

$$\frac{R}{R_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right) \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}$$

Stello et al. (2008; ApJL 674, L53)  
Kallinger et al. (2010; A&A 509, A77)

for uncertainties on  $T_{\text{eff}}$  see, e.g.,  
Tayar et al. (2022)





# 1. The $v_{max}$ scaling relation

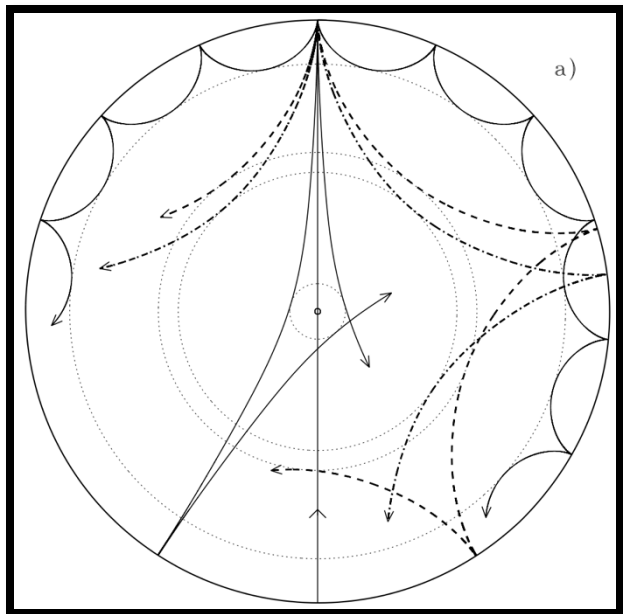
$$\frac{v_{max}}{v_{max,\odot}} \approx \frac{g}{g_{\odot}} \left( \frac{T_{eff}}{T_{eff,\odot}} \right)^{-1/2}$$

# 1. The $\nu_{max}$ scaling relation

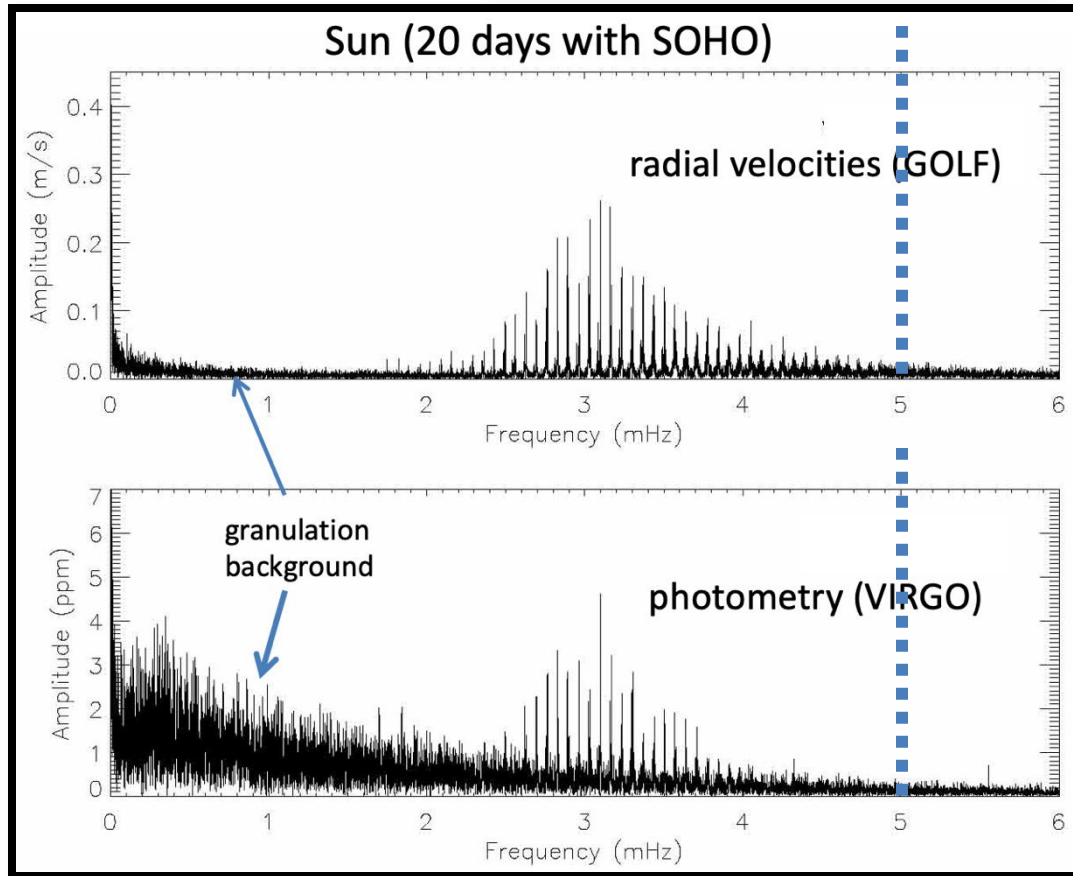
$$\frac{\nu_{max}}{\nu_{max,\odot}} \approx \frac{g}{g_{\odot}} \left( \frac{T_{eff}}{T_{eff,\odot}} \right)^{-1/2}$$

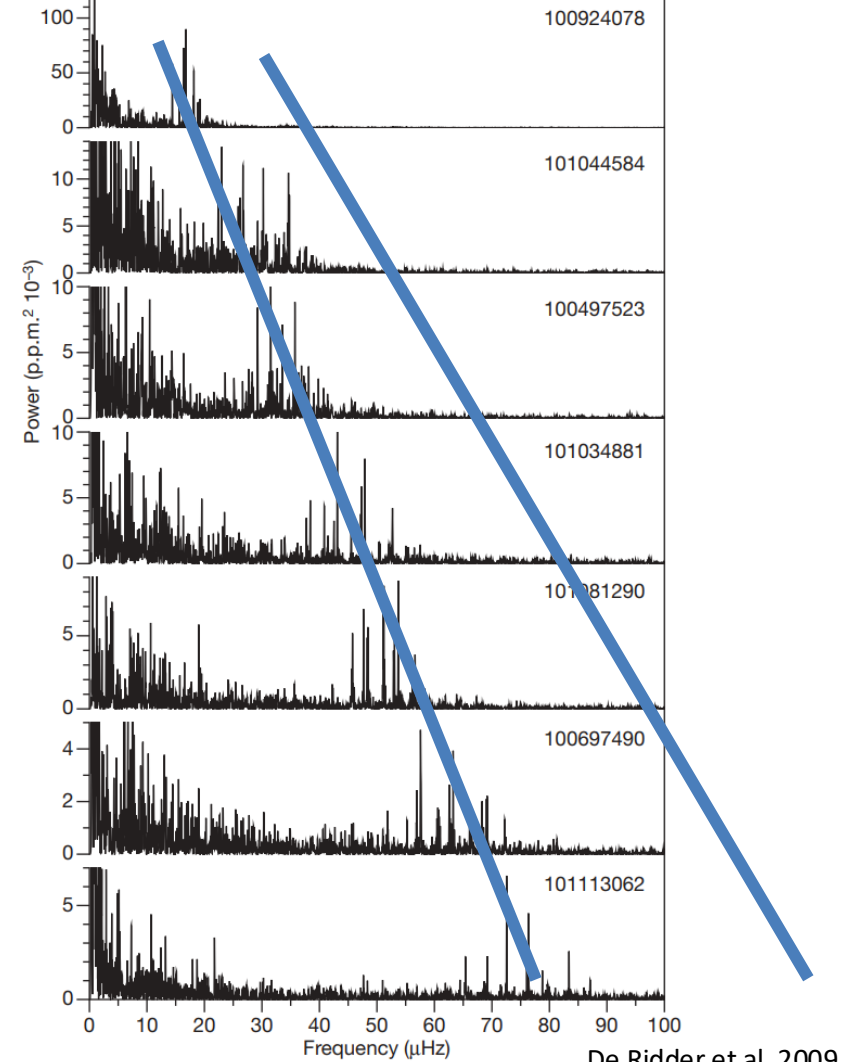
$$\nu_{ac} \propto g / \sqrt{T_{eff}}$$

Brown et al. (1991);  
Kjeldsen & Bedding (1995)



Aerts et al. (2011)





We extrapolate from the Sun, assuming  $\nu_{max}$  is a *fixed fraction* of the acoustic cutoff frequency ( $\sim 0.6$ ).

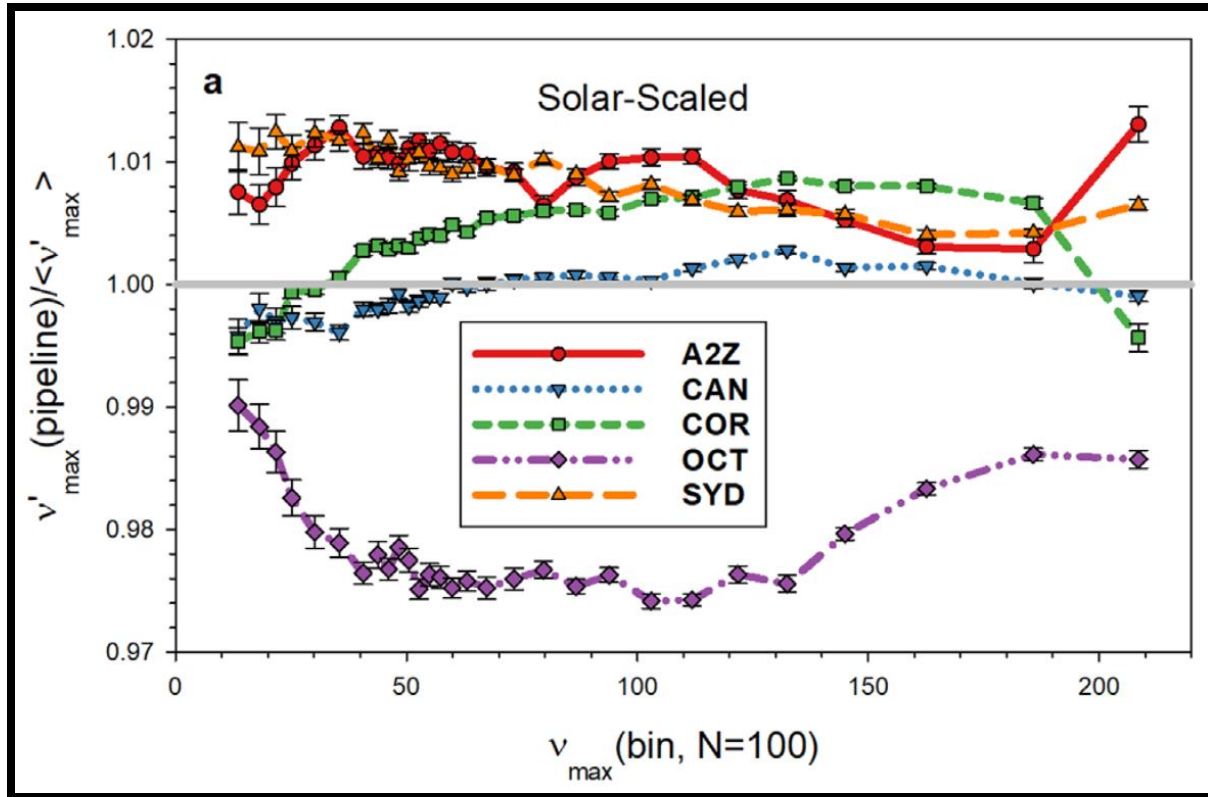
$$\nu_{max} \propto \nu_{ac} \propto g / \sqrt{T_{eff}}$$

Brown et al. (1991);  
Kjeldsen & Bedding (1995)

Introduced to *predict*  $\nu_{max}$ .

see e.g.,  
 Belkacem et al. (2011; A&A)  
 Bedding (2014; arxiv:1107.1723)  
 Chaplin & Miglio (2013, ARAA)  
 Hekker (2019; *Frontiers*)  
 Yaguang Li et al. (2021)

# $V_{max}$ depends on how you measure it



For red giants (APOKASC;  
Pinsonneault et al. 2018)

Same is true for dwarfs  
(e.g., Verner et al. 2011)

# The $\nu_{max}$ scaling probably depends on metallicity

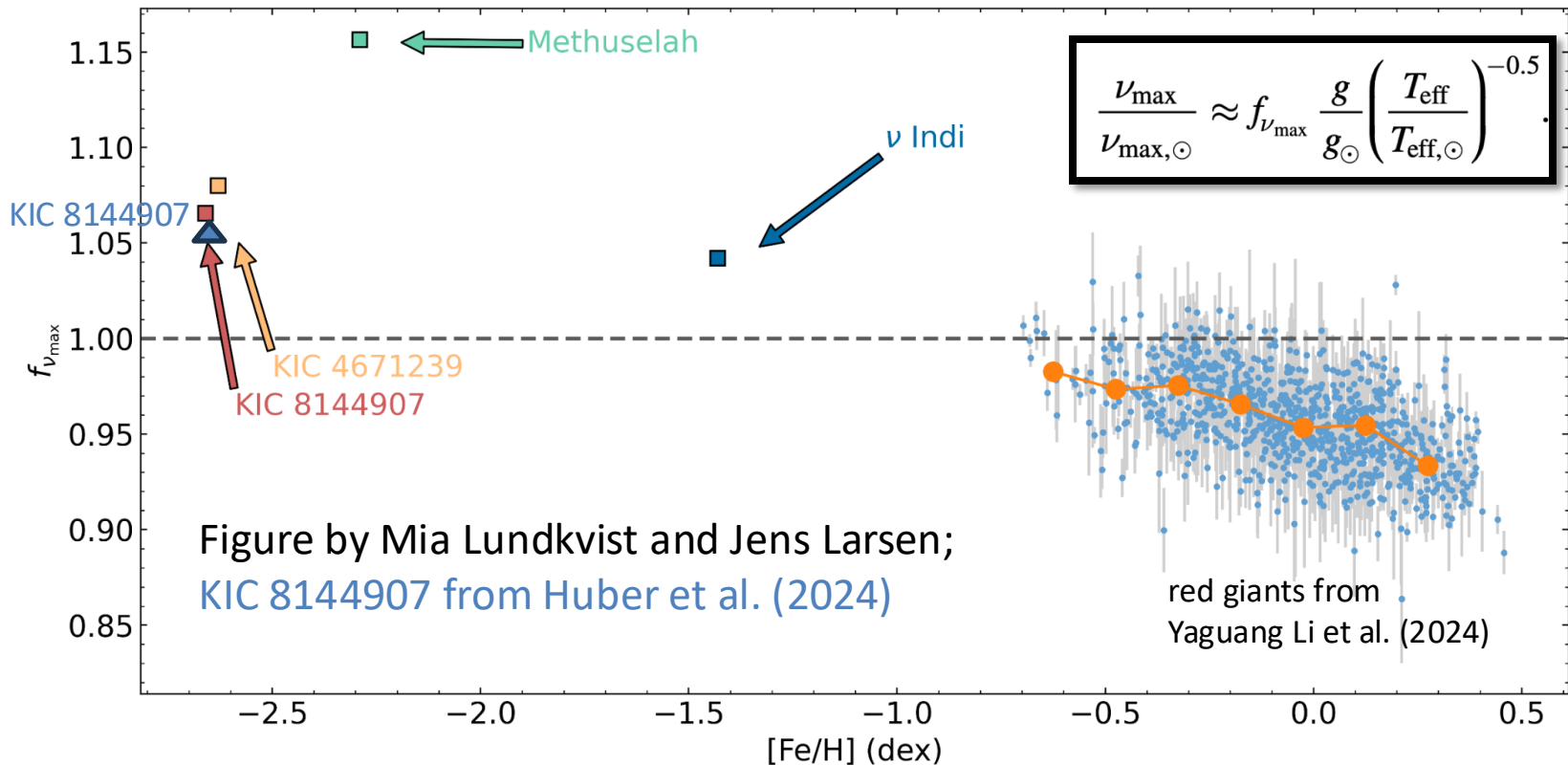


Figure by Mia Lundkvist and Jens Larsen;  
KIC 8144907 from Huber et al. (2024)

red giants from  
Yaguang Li et al. (2024)

see also Vianni et al. (2017); Yixiao Zhou et al (2024)

# Asteroseismic scaling relations:

1.  $\nu_{\max}$  depends on surface properties (excitation & damping of modes):

$$\frac{\nu_{\max}}{\nu_{\max,\odot}} \approx \frac{g}{g_{\odot}} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{-1/2}$$

2.  $\Delta\nu$  scales with sqrt[mean density] (sound travel time across star):

$$\Delta\nu \propto \left( \frac{M}{R^3} \right)^{1/2}$$

Solve to get mass and radius:

$$\frac{M}{M_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right)^3 \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-4} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{3/2}$$

$$\frac{R}{R_{\odot}} \simeq \left( \frac{\nu_{\max}}{\nu_{\max,\odot}} \right) \left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right)^{-2} \left( \frac{T_{\text{eff}}}{T_{\text{eff},\odot}} \right)^{1/2}$$

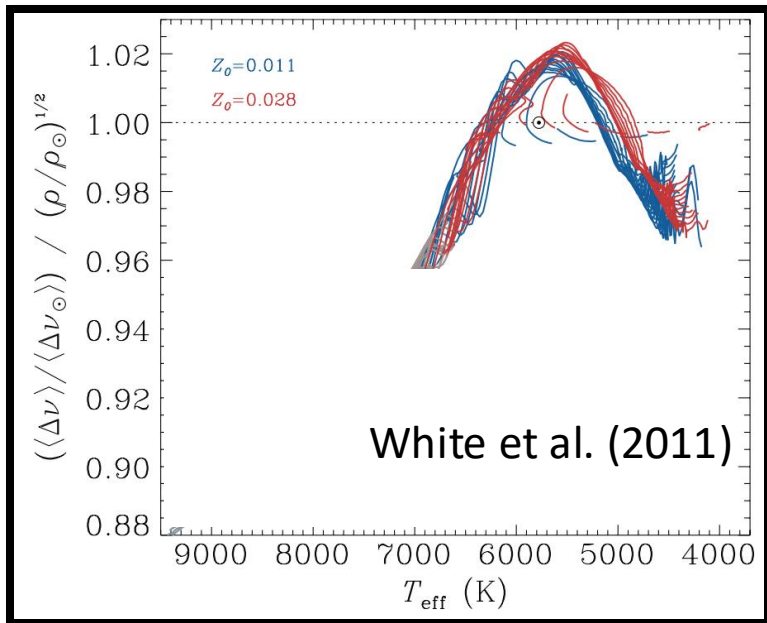
Stello et al. (2008; ApJL 674, L53)  
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for uncertainties on  $T_{\text{eff}}$  see, e.g.,  
Tayar et al. (2022)

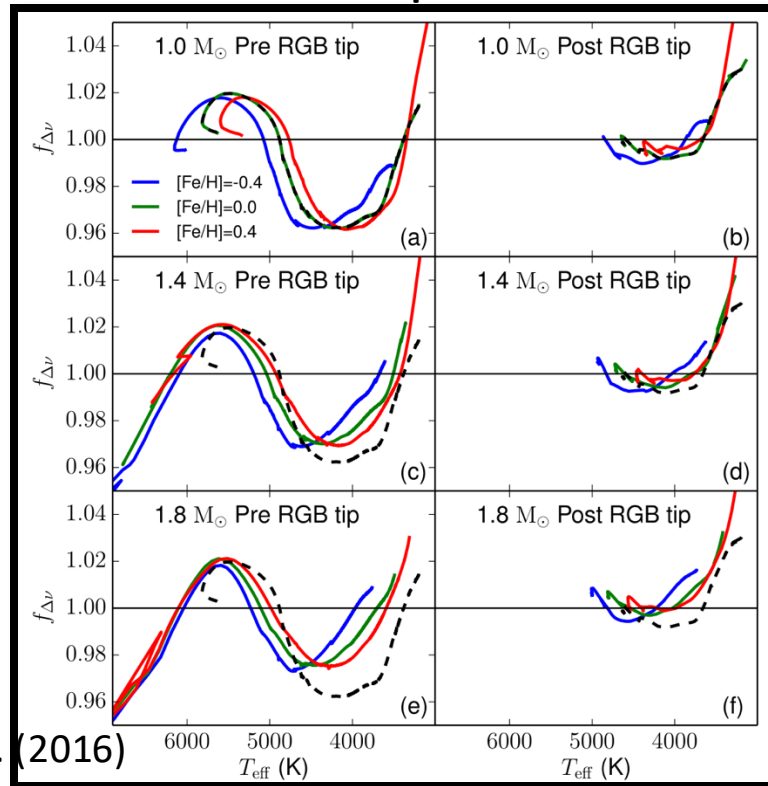
## 2. The $\Delta\nu$ scaling relation

$$\left(\frac{\Delta\nu}{\Delta\nu_{\odot}}\right) = f_{\Delta\nu} \left(\frac{\rho}{\rho_{\odot}}\right)^{0.5}$$

- relies on solid theory (we can compute oscillation frequencies using models)



Sharma et al. (2016)





# A prescription for the asteroseismic surface correction (2023)

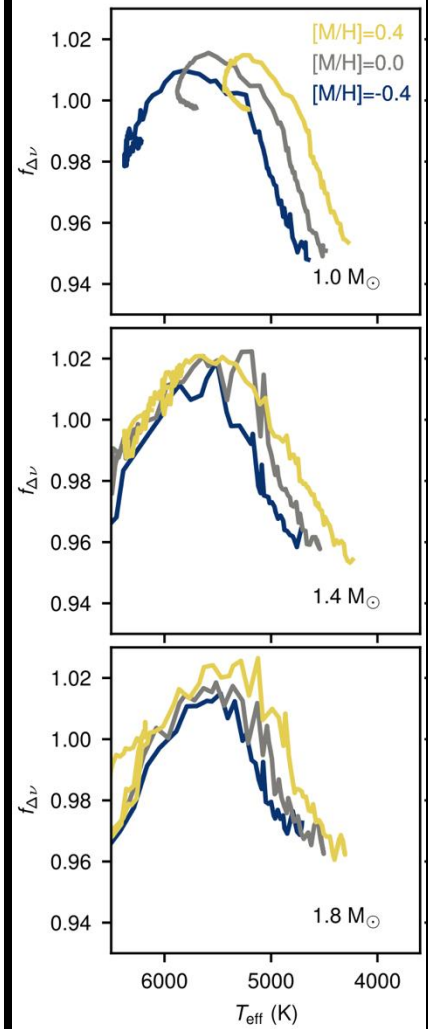
Yaguang Li, (李亚光)<sup>1\*</sup>, Timothy R. Bedding<sup>1</sup>, Dennis Stello<sup>1,2,3</sup>, Daniel Huber<sup>4</sup>, Marc Hon<sup>4</sup>,  
 Meridith Joyce<sup>5</sup>, Tanda Li, (李坦达)<sup>6</sup>, Jean Perkins<sup>7</sup>, Timothy R. White<sup>1</sup>, Joel C. Zinn<sup>8</sup>,  
 Andrew W. Howard<sup>9</sup>, Howard Isaacson<sup>10</sup>, Daniel R. Hey<sup>4</sup> and Hans Kjeldsen<sup>3</sup>

$$\left( \frac{\Delta\nu}{\Delta\nu_{\odot}} \right) = f_{\Delta\nu} \left( \frac{\rho}{\rho_{\odot}} \right)^{0.5}$$

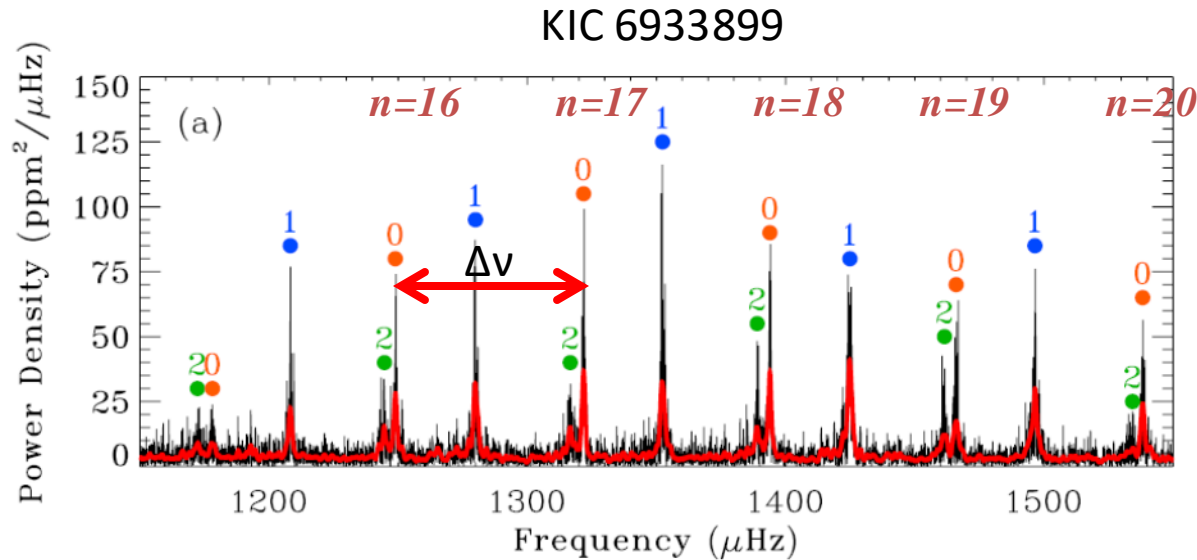
$$\begin{aligned} f_{\Delta\nu} = & \beta_0 + \beta_1 \log_{10}(\nu_{\max}/3090 \mu\text{Hz}) \\ & + \beta_2 \log_{10}(\Delta\nu/135.1 \mu\text{Hz}) \\ & + \beta_3 (T_{\text{eff}}/5777 \text{ K}) \\ & + \beta_4 (T_{\text{eff}}/5777 \text{ K})^2 \\ & + \beta_5 (T_{\text{eff}}/5777 \text{ K})^3 \\ & + \beta_6 [\text{M}/\text{H}], \end{aligned}$$

for  $0.8 < M/M_{\odot} < 2.2$ ,  $-0.8 < [\text{M}/\text{H}] < 0.5$ ,  
 and pre-RGB tip ( $\Delta\nu > 2.0 \mu\text{Hz}$ ).

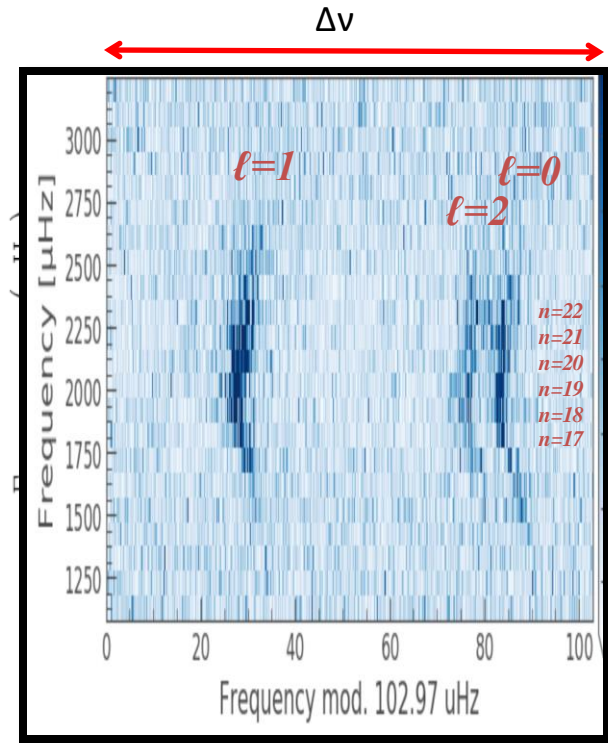
(16)



# Better to make full use of *all* the mode frequencies



White et al. (2012)



échelle diagram

# Summary

- $v_{\max}$  scaling relation is surprisingly good (few percent), but has metallicity dependence (and value depends on method)
- $\Delta v$  scaling relation is very good with theoretical corrections (including the surface correction; see Yaguang Li et al. 2023)
- Best practice: fit the individual mode frequencies (and maybe include  $v_{\max}$  as an extra constraint)