Extracting the Full Cosmological Information of Roman

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Challenging Theory with Roman - July 11, 2024

the standard ACDM model of cosmology



image: NASA

the standard Λ CDM model of cosmology



image: NASA

the standard ACDM model of cosmology



image: NASA

the standard ACDM model of cosmology



the standard Λ CDM model of cosmology is remarkably successful at describing current observations



image: Planck

the standard Λ CDM model of cosmology



cosmic tensions











spectroscopic galaxy surveys probe both the growth of structure and the expansion rate

image: Sloan Digital Sky Survey

spectroscopic galaxy surveys provide photometry

spectroscopic galaxy surveys provide photometry and spectra of galaxies



spectroscopic galaxy surveys map the detailed three-dimensional spatial distribution of galaxies

1612

12h

image: Michael Blanton, SDSS

$$z_{\rm obs} = z_{\rm cosmo} + \frac{v_{\rm pec}}{c}$$

cosmological expansion

$$z_{obs} = z_{cosmo} + \frac{v_{pec}}{c}$$
peculiar velocity









image: Eke et al. (2003)













galaxy overdensity in redshift-space $\delta_g^{(s)}(k)$

 $\delta_g^{(s)}(k) = \delta_g(k)$ galaxy overdensity in real-space

**linear theory*

$$\delta_g^{(s)}(k) = \delta_g(k) + f\mu^2 \delta_m(k)$$

growth rate of structure matter overdensity

$$\delta_g^{(s)}(k) = \delta_g(k) + f\mu^2 \delta_m(k)$$
$$P_g^{(s)}(k) = \langle \delta_g^{(s)}(k) \delta_g^{(s)}(k') \rangle$$
$$= \left(b + f\mu^2\right)^2 P_m(k)$$

galaxy power spectrum

**linear theory*



SDSS — Beutler et al.(2017), Gil-Marín et al.(2020)

3D distribution of galaxies encodes cosmological information on the **expansion history** from Baryon Acoustic Oscillations (BAO)

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2pt correlation function $\xi \equiv$ Fourier transform of P_g

BOSS — Sanchez et al. (2013)

3D distribution of galaxies encodes cosmological information on the **expansion history** from Baryon Acoustic Oscillations (BAO)



BOSS - Sanchez et al. (2013)

3D galaxy distribution encodes cosmological information on the **growth** and **expansion history** of the Universe

current analyses

Salaxy surveys

current galaxy clustering analyses only use the **power spectrum** on large **linear scales**



SDSS — Beutler et al.(2017), Gil-Marín et al.(2020)
current galaxy clustering analyses only use the **power spectrum** on large **linear scales**



SDSS — Beutler et al.(2017), Gil-Marín et al.(2020)



Sefusatti et al.(2005)

these two distributions have the *same* power spectrum



Sefusatti et al.(2005)

these two distributions have the *same power spectrum* but very different *higher-order clustering*



Sefusatti et al.(2005)

how much cosmological information is available *beyond the power spectrum*?



82,000 full *N*-body simulations *Villaescusa-Navarro*, *Hahn et al.* (2019)





75,000 simulated galaxy catalogs *Hahn & Villaescusa-Navarro (2021)*



with the bispectrum we can constrain the Λ CDM parameters $(\Omega_m, \Omega_b, h, n_s, \sigma_8) \gtrsim 3 \times$ tighter than the power spectrum alone

Hahn et al. (2020) Hahn & Villaescusa-Navarro (2021) significant cosmological information on non-linear scales



many promising clustering statistics beyond the power spectrum -e.g.



current analyses

higher-order and *non-linear* cosmological information



challenges: analytic models of galaxy clustering are *inaccurate* on non-linear scales $k_{\text{max}} \gtrsim 0.2 \, h/\text{Mpc}$



Chudaykin & Ivanov (2019)

challenges: analytic models of galaxy clustering are *inaccurate* on non-linear scales $k_{\text{max}} \gtrsim 0.2 \, h/\text{Mpc}$



no analytic models available for - e.g. wavelet statistics, k^{th} -nearest neighbor, minimum spanning tree...

challenges: observations are messy



SDSS-III: BOSS CMASS Southern Galactic Cap

challenges: observations are messy - e.g. fiber collisions strongly affect small scale clustering



no correction scheme currently available for higher-order statistics

current challenges for clustering using higher-order statistics on nonlinear scales

1. modeling *non-linear* scales

2. modeling clustering statistics beyond P_{ℓ}

3. observational systematics

current challenges can be addressed with a simulation-based approach

1. modeling non-linear scales

N-body simulations can accurately model small scales

2. modeling clustering statistics beyond P_{ℓ}

we can use any statistic that can be measured in observations

3. observational systematics

we already have forward models of geometry, fiber collisions, etc





 $p(\begin{array}{c} \Omega_m, \Omega_b, h \\ n_s, \sigma_8 \end{array} |$

 ΛCDM parameters



$$p(\Omega_m,\Omega_b,h) | = n_s,\sigma_8 | = p(\Omega_m,\Omega_b,\sigma_8) | = p$$

using simulation-based inference



















the forward model/simulator implicitly defines our likelihood



the forward model/simulator implicitly defines our likelihood



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the forward model/simulator implicitly defines our likelihood



the forward model/simulator implicitly defines our likelihood









$$p(\theta \mid \mathbf{X}_{obs}) \approx p(\theta \mid X \approx \mathbf{X}_{obs})$$


what is **simulation-based inference**?

$$p(\theta \mid \mathbf{X}_{obs}) \approx p(\theta \mid X \approx \mathbf{X}_{obs})$$



SBI 101 — approximate bayesian computation

simulation-based inference in practice



SBI 101 — approximate bayesian computation

simulation-based inference in practice



approximate bayesian computation is often *infeasible*

simulation-based inference *in practice* — density estimation



some model q with free parameters ϕ

*Gaussian Mixture Models, Independent Component Analysis, neural density estimators...

we can determine ϕ by

$\min_{\phi} D_{\mathrm{KL}}(p(\theta \mid \mathbf{X}) p(\mathbf{X}) \parallel q_{\phi}(\theta \mid \mathbf{X}) p(\mathbf{X}))$

Kullback-Leibler divergence (a.k.a. relative entropy)

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$\min_{\phi} D_{\mathrm{KL}}(p(\theta \mid \mathbf{X}) p(\mathbf{X}) \parallel q_{\phi}(\theta \mid \mathbf{X}) p(\mathbf{X}))$



$$\min_{\phi} D_{\mathrm{KL}}(p(\theta \mid \mathbf{X}) p(\mathbf{X}) \parallel q_{\phi}(\theta \mid \mathbf{X}) p(\mathbf{X})$$
$$= \min_{\phi} \int p(\theta \mid \mathbf{X}) p(\mathbf{X}) \log \frac{p(\theta \mid \mathbf{X}) p(\mathbf{X})}{q_{\phi}(\theta \mid \mathbf{X}) p(\mathbf{X})}$$

Kullback-Leibler divergence (a.k.a. relative entropy)

we can determine ϕ by

$$\min_{\phi} D_{\mathrm{KL}}(p(\theta \mid \mathbf{X}) p(\mathbf{X}) \parallel q_{\phi}(\theta \mid \mathbf{X}) p(\mathbf{X}))$$
$$= \min_{\phi} \int_{p(\theta \mid \mathbf{X}) p(\mathbf{X})}^{p(\mathbf{X}, \theta)} \log \frac{p(\theta \mid \mathbf{X}) p(\mathbf{X})}{q_{\phi}(\theta \mid \mathbf{X}) p(\mathbf{X})}$$









we can determine ϕ by

 $\begin{array}{l} q_{\phi}(\theta \,|\, \mathbf{X}) \text{ is guaranteed to converge to } p(\theta \,|\, \mathbf{X}) \text{ if} \\ \\ q_{\phi} \text{ is flexibly expressive} \\ \\ N \rightarrow \infty \text{ samples from } p(\mathbf{X}, \theta) \\ \\ \text{ successful optimization} \end{array}$

$$= \max_{\phi} \sum_{(\mathbf{X}', \theta') \sim p(\mathbf{X}, \theta)} \log q_{\phi}(\theta' \mid \mathbf{X}')$$



image: Janosh Riebesell



 $z_i = f_i(z_{i-1})$ are invertible and differentiable transformations

$$p(z_i) = p(z_{i-1}) \left| \det\left(\frac{\partial f_i^{-1}}{\partial z_i}\right) \right|$$



 $z_i = f_i(z_{i-1})$ are invertible and differentiable transformations

 $f = f_1 \circ f_2 \dots \circ f_{k-1} \circ f_k$ is also invertible and differentiable



Yang et al.(2019) PointFlow

 $p(\begin{array}{c} \Omega_m, \Omega_b, h \\ n_s, \sigma_8 \end{array} |$



 $\Lambda \text{CDM} parameters$

observed galaxy distribution



Simulation-Based Inference of Galaxies









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https://changhoonhahn.github.io/simbig/

SIMBIG – 1. generating training data of synthetic observations



SIMBIG – 2. *training the normalizing flow*



SIMBIG - 3. inference using real observations





SIMBIG - 3. inference using real observations



SIMBIG - 3. inference using real observations



SIMBIG – 3. inference using real observations





Quijote high-res N-body simulations



Quijote high-res *N*-body simulations



Rockstar phase-space halo finder



Quijote high-res N-body simulations



Rockstar phase-space halo finder



HOD model with assembly, velocity, concentration biases



Quijote high-res N-body simulations



Rockstar phase-space halo finder



HOD model with assembly, velocity, concentration biases



survey realism: redshift-space, geometry, mask, fiber collisions



20,000 training simulations spanning broad range of cosmologies and HOD parameters

Hahn et al.(2023c, 2023d)





Model

Hahn et al.(2023c, 2023d) video: Bruno Régaldo-Saint Blancard

SIMBIG: non-linear galaxy power spectrum $P_{\ell}(k < 0.5 h/Mpc)$

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Hahn et al.(2023c); Hahn et al.(2023d) PNAS

SIMBIG: non-linear galaxy power spectrum $P_{\ell}(k < 0.5 h/\text{Mpc})$



Hahn et al.(2023c); Hahn et al.(2023d) PNAS
SIMBIG: non-linear galaxy bispectrum $B_0(k_1, k_2, k_3 < 0.5 h/Mpc)$

SIMBIG: non-linear galaxy bispectrum $B_0(k_1, k_2, k_3 < 0.5 h/Mpc)$



1.2 and 2.4 \times tighter Ω_m and σ_8 from **non-linear** + **higher-order** clustering

Hahn et al. (2023h)



Liam Parker Princeton Univ.



Pablo Lemos MILA

SIMBIG: convolutional neural network field-level summary



extracting all relevant cosmological information in N-pt functions

Lemos, Parker, Hahn et al. (2023)



Liam Parker Princeton Univ.



Pablo Lemos MILA

SIMBIG: convolutional neural network field-level summary



extracting all relevant cosmological information in N-pt functions

Parker, Lemos, Hahn et al. (2023)



wavelet scattering transforms

Régaldo-Saint Blancard, Hahn et al. (2023)

skew spectra Hou, Moradinezhad Dizgah, **Hahn** et al. (2024)



Bruno Régaldo-Saint Blancard CCM Flatiron



Jiamin Hou Univ. of Florida

marked powerspectrum Massara, **Hahn** et al. (2024)



Elena Massara UWaterloo

voids, graph neural network, combined ... coming soon

SIMBIG: ~1.9 and 1.5× tighter S_8 and H_0



SIMBIG: ~1.9 and 1.5× tighter S_8 and H_0



production level cosmological constraints — not a proof-of-concept!

Hahn et al. (2023i)

SIMBIG: ~1.9 and 1.5× tighter S_8 and H_0



 S_8 improvement is equivalent to analyzing a survey of ~4× larger volume

Hahn et al. (2023i)

~100,000 galaxies at $z \sim 0.5$

Salaxy surveys

~100,000 galaxies at $z \sim 0.5$



Roman High Latitude Spectroscopic Survey

~10 million H α Emission-Line Galaxies 1 < z < 2

~2 million OIII Emission-Line Galaxies



Wang et al. (2022)



adapted from Hahn et al. (2023i)

SIMBIG + DESI and *Roman* will probe *new regimes*



adapted from Hahn et al. (2023i)

SIMBIG + DESI and *Roman* will probe *new regimes*



adapted from Hahn et al. (2023i)

SIMBIG + DESI and Roman will probe new regimes



galaxy surveys encode the growth and expansion histories of the Universe

ML×Cosmo: SIMBIG analyses leverage *non-linear* and *higher-order* galaxy clustering to **double** the cosmological impact of galaxy surveys

Roman with SIMBIG will settle cosmic tensions and probe new physics

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